$\frac{3}{2}$  3  $\frac{1}{2}$  3  $\frac{3}{2}$  3  $\frac{1}{2}$  3  $\frac{1$  $4$  – Experimenting with neurosymbolic  $A$  For  $4$  $\mathbb{E}_{\mathbf{S}}$  Experimenting with neurosymbolic AI for  $\frac{6}{9}$  defending example  $\frac{1}{2}$  and  $\frac{1}{2}$  defending **defending against cyber attacks** 

 $1$  $2 \times 2$ 

<span id="page-0-0"></span>8 a set of the set of th <sup>9</sup> Magnus Wiik Eckhoff <sup>[a,](#page-0-0)[b](#page-0-1)</sup>, Jon[a](#page-0-0)s Halvorsen <sup>a</sup>, Bjørn Jervell Hansen <sup>a</sup>, Martin Eian <sup>[c](#page-0-2)</sup>,

<span id="page-0-2"></span><span id="page-0-1"></span><sup>10</sup> Vasileios Mavroeidis <sup>[b](#page-0-1)</sup>, Robert Andrew Chetwyn <sup>b</sup>, Geir Skjøtskift <sup>[c](#page-0-2)</sup> and Gudmund Grov <sup>[a,](#page-0-0)[b,](#page-0-1)[\\*](#page-0-3)</sup> 11 11 <sup>a</sup> *Norwegian Defence Research Establishment (FFI), Norway* 12 12 *E-mails: [Magnus-Wiik.Eckhoff@ffi.no,](mailto:Magnus-Wiik.Eckhoff@ffi.no) [Jonas.Halvorsen@ffi.no,](mailto:Jonas.Halvorsen@ffi.no) [Bjorn-Jervell.Hansen@ffi.no,](mailto:Bjorn-Jervell.Hansen@ffi.no)* 13 13 *[Gudmund.Grov@ffi.no](mailto:Gudmund.Grov@ffi.no)* 14 14 <sup>b</sup> *Department of Informatics, University of Oslo, Norway* 15 15 *E-mails: [vasileim@ifi.uio.no,](mailto:vasileim@ifi.uio.no) [roberac@ifi.uio.no](mailto:roberac@ifi.uio.no)* 16 16 <sup>c</sup> *mnemonic, Norway* 17 17 *E-mails: [meian@mnemonic.no,](mailto:meian@mnemonic.no) [geir@mnemonic.no](mailto:geir@mnemonic.no)* 18 18 19 19  $20$ 21  $\sim$  21 22 **Abstract.** It is generally accepted that all cyber attacks cannot be prevented, which creates a need for the ability to detect and 22 <sub>23</sub> respond to cyber attacks. Both connectionist and symbolic approaches are currently being used to support such detection and <sub>23</sub>  $_{24}$  response. This paper makes the case for combining the two using neurosymbolic AI. We identify a set of challenges faced  $_{24}$ 

 $_{25}$  when using AI today and propose a set of neurosymbolic use cases we believe are both interesting research directions for the  $_{25}$ neurosymbolic AI community and can have an impact on the cyber security field. We demonstrate feasibility through several  $_{26}$  $27$  at the NeSy 2024 conference [\[42\]](#page-26-0). The main additional contributions are further experimental evidence for our hypothesis that <sup>28</sup> NeSy offers real benefits in this domain and a more in-depth treatment of knowledge graphs for cyber security.<sup>28</sup> experiments applying neurosymbolic AI to cyber security challenges. This paper is an extended version of a paper published

 $29$ 

 $31$   $31$  $32$  32 33 33  $34$ 

30 30 Keywords: AI, neurosymbolic AI, cyber security, incident detection and response

#### 35 35  $\frac{36}{36}$  **1. INTOURCION** 36 1. Introduction

 $37$ Protecting assets in the cyber domain requires a combination of *preventive measures*, such as access control and firewalls, and the ability to *defend* against cyber operations when the preventive measures were not sufficient.<sup>[1](#page-0-3)</sup>

Our focus in this paper is on defending against offensive cyber operations, and before going into details, some  $\frac{40}{40}$  $\frac{41}{41}$  concepts and terminology need to be in place:

42 42 Terminology & concepts The focus of this paper is to defend *assets* against *threats* in cyberspace. An *as-*<sup>43</sup> *set* can be anything from information or physical infrastructure and people to the internal processes of an <sup>43</sup> 44 44 enterprise. *Threats* manifest themselves in the form of *cyber operations* (or *cyber attacks*) conducted by an 45 45 *adversary* (or *threat actor*). In our context of defending, the term *incident* is used for a potential attack that <sup>46</sup> is deemed to have an impact on assets, and the process of defending comes under the area of *incident man*-47 47

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49 49 \*Corresponding author. E-mail: [Gudmund.Grov@ffi.no.](mailto:Gudmund.Grov@ffi.no)

<span id="page-0-3"></span> $1$ It is generally accepted that preventive measures are not sufficient in cyberspace. An analogy is that we still need smoke detectors and a  $50$ 51 51 fire brigade, even if we take all possible preventive measures to reduce the risk of a fire.

 1 *agement* [\[22\]](#page-26-1). This is typically conducted in a *security operations centre* (SOC), which consists of people, 2 processes, and tools. One of the objectives of a SOC is to detect and respond to threats and attacks, where 3 *security analysts* play a crucial role. Knowledge of threats in the cyber domain is developed by conducting 4 intrusion analysis and producing and consuming *cyber threat intelligence* (CTI). Networks and systems to be 5 protected are monitored, and *events* – e.g., network traffic, file changes, or processes executing on a host – 6 are forwarded and typically stored in a *security information and event management* (SIEM) system, where 7 events can be investigated, correlated and enriched, and queried. We will use the term *observations* for such 8 events resulting from monitoring. Suspicious activity that is observed may raise *alerts*, which may indicate an 9 incident that has to be analysed and responded to in the SOC. Finally, *Neurosymbolic AI* [\[37\]](#page-26-2), which aims to 10 combine connectionist and symbolic AI, will be abbreviated *NeSy*.

<sup>12</sup> Why is a SOC relevant for NeSy? A SOC essentially conducts abductive reasoning by observing traces and iden-<sup>13</sup> tifying and analysing their cause in order to respond. This involves sifting through masses of events for suspicious <sup>13</sup>  $14$  behaviour, an area in which extensive research has been conducted for several decades using statistics and machine  $14$ 15 15 learning. Identifying the cause of observed suspicious behaviour requires situational awareness, achieved by com-<sup>16</sup> bining and reasoning about different types of knowledge. There are various ways knowledge is represented, such<sup>16</sup> <sup>17</sup> as structured events and alerts, unstructured reports, and semantic knowledge [\[66,](#page-27-0) [100\]](#page-28-0). In a SOC, the ability to 18 18 *learn* models to detect suspicious activities, and the ability to *reason* about identified activity from such models to understand their cause and respond, is thus required. These abilities are at the core of NeSy, and our hypothesis is:

 $11$  11  $\overline{11}$  11

# 21 21 *A SOC provides an ideal environment to study NeSy with great potential for both scientific and financial impact.*

22  $\sim$  22 23 Some early work has explored NeSy in the cyber security domain [\[28,](#page-26-3) [48,](#page-27-1) [51,](#page-27-2) [83,](#page-28-1) [88\]](#page-28-2) and our goal with this paper,  $_{23}$  $_{24}$  which extends [\[42\]](#page-26-0), is to showcase the possibilities and encourage the NeSy community to conduct research in the  $_{24}$ 25 SOC field with an emphasis on experiments. 25 25

26  $\sim$  26 *27 Methodology:* The identified SOC challenges are derived from a combination of existing published studies, the experience and expertise of the authors, and further discussions with SOC practitioners. The use cases result from  $_{28}$  $_{29}$  reviewing NeSy literature in the context of the identified challenges, and the preliminary experiments conducted are  $_{29}$  $30 \text{ based on a subset of the identified use cases.}$ 

<sup>31</sup> *Paper structure:* In [§2,](#page-2-0) we describe the typical use of AI in a SOC and the identified challenges. In [§3,](#page-4-0) we make 32 32 the case for NeSy and outline the NeSy use cases. In [§4,](#page-8-0) we describe the proof-of-concept experiments, before we  $\frac{33}{33}$  $\frac{34}{34}$  conclude in  $\zeta$ .  $\frac{34}{34}$ conclude in [§5.](#page-25-0)

<sup>35</sup> *Contributions:* This paper is an extended version of [\[42\]](#page-26-0), published at the NeSy 2024 conference. We outline how  $\frac{36}{25}$  AI is used today in a SOC and identify and structure a set of challenges faced by practitioners who use AI. We then  $\frac{37}{2}$  37  $\frac{37}{2}$   $\frac{37}{2}$   $\frac{37}{2}$   $\frac{37}{2}$   $\frac{37}{2}$   $\frac{37}{2}$   $\frac{37}{2}$   $\frac{37}{2}$ create a set of promising use cases for applying NeSy in the context of a SOC, review current NeSy approaches in ight of them, and demonstrate feasibility through proof-of-concept experiments. In this paper, we extend [\[42\]](#page-26-0) with  $\frac{39}{39}$  $_{40}$  a more profound treatment of the use of knowledge graphs when defending against cyber attacks, and, crucially, we address the main limitation of  $[42]$  – limited experimental evidence – with the following experiments:

- 42 42 Our experiment with *Logic Tensor Networks (LTN)* [\[12\]](#page-25-1) in [\[42\]](#page-26-0) is replaced with using LTN with a published ML 43 43  $\frac{44}{44}$  model for network introduction detection [\[95\]](#page-28-3), and extended with further experiments addressing explainability aspects and prioritising crucial knowledge.  $45$
- <sup>46</sup> A NeSy technique called *Embed2Sym* [\[10\]](#page-25-2) is explored to analyse and contextualise alerts from intrusion detec- $\frac{47}{47}$  47 tion systems.
- 48 48 Building on [\[19,](#page-26-4) [21\]](#page-26-5), we explore the integration of large language models with a symbolic approach for *threat*  $49$  hunting.  $49$ *hunting*.

50 50 – We extend our previous work using data-driven enrichment of (symbolic) knowledge [\[101\]](#page-28-4) with experiments 51 51 using newly released data and explore the advantages NeSy provides for this challenge.

# <span id="page-2-0"></span>1 **2. Challenges faced when using AI in a SOC**  $\frac{1}{2}$

3 3 MAPE-K (Monitor-Analyse-Plan-Execute over a shared Knowledge) [\[56\]](#page-27-3) is a common reference model to struc-<sup>4</sup> ture the different phases when managing an incident.<sup>[2](#page-2-1)</sup> For each phase of MAPE-K, we below discuss the common 5 5 use of AI, including underlying representations, and identify key challenges security practitioners face when using  $\rm A I$ .<sup>3</sup> 6  $AI.<sup>3</sup>$  $AI.<sup>3</sup>$  $AI.<sup>3</sup>$ 

7 and  $\sim$  7 *8 Monitor* In the *monitor* phase, systems and networks are monitored and telemetry is represented as sequences of *events*. An *event* could, for instance, be a network packet, a file update, a user that logs on to a service, or a 10 Process componented Events are cypremy subvented as ney value pairs. For a large enterprise, who or allowships of events may be generated per second. In this phase, a key objective is to detect suspicious behaviours from events  $\frac{1}{11}$ process being executed. Events are typically structured as key-value pairs. For a large enterprise, tens of thousands and generate *alerts*, which are analysed and handled in the later phases of MAKE-K.

 $\frac{12}{12}$  This is a topic where machine learning (ML) has been extensively studied by training ML models on the vast 13<br>amount of captured event data (see e.g. [\[5\]](#page-25-3)). A challenge with such data is the lack of *ground truth*, in the sense 14 announced by the data (see e.g. [b]). It entirely what seem data is the fact of ground brand, in the sense that for the vast majority of events we do not know if they are benign or malicious. As most events will be benign  $\frac{15}{15}$ (albeit we do not know which ones), one can exploit this assumption and use unsupervised methods to train anomaly 17 december 2011 a common approach. For all base research parposes, symmetre datasets from simulated attaches are also commonly used [\[58\]](#page-27-4). However, synthetic datasets suffer from several issues [\[9,](#page-25-4) [55\]](#page-27-5) and promising results in research papers using synthetic data tend not to be recreated in real-world settings – whilst anomaly detectors often  $\frac{19}{19}$ create a high number of false alerts<sup>[4](#page-2-3)</sup> [\[17,](#page-26-6) [102\]](#page-28-5). Our first challenge, which follows from the *European Union Agency for Cybersecurity* (ENISA) [\[33\]](#page-26-7), addresses this performance issue for ML models for real-world conditions: detectors. This is a common approach. For at least research purposes, synthetic datasets from simulated attacks are

# <span id="page-2-5"></span>22 22 Challenge 1. *Achieve optimal accuracy of ML models under real-world conditions.*

 $23$  23 24 As benign software and malware are continuously updated, the notion of *concept drift* is prevalent, and ML <sub>24</sub>  $_{25}$  models must thus be retrained regularly. Moreover, in addition to the large amount of data, requiring scalability,  $_{25}$ real-world conditions will have a large amount of noise (i.e. aleatoric uncertainty) in the data, which is not well  $\frac{27}{27}$  checked in symmetre data. reflected in synthetic data.

28 28 28 28 For previous incidents that have been handled, we know the ground truth of the associated alerts and events.  $_{29}$  Compared with the full set of events, this dataset will, however, be tiny. Still, it is important as it is labelled and  $_{29}$  $_{30}$  contains data we know are relevant – either in terms of actual attacks experienced or false alerts that should be  $_{31}$  filtered out. One important challenge, also identified by ENISA [\[33\]](#page-26-7), is the ability to exploit such labelled "incident  $_{31}$  $32$  datasets" and train ML models based on them:

<span id="page-2-6"></span>33 33 Challenge 2. *Learning with small (labelled) datasets (from cyber incidents).*

 $\frac{34}{25}$  New knowledge about certain threats, attacks, malware, or vulnerability exploits is frequently published (e.g. <sup>35</sup> threat reports). The traditional, and still most common, method of threat detection is so-called *signature-based* <sup>36</sup> detection, where such knowledge is (often manually) encoded as specific patterns (called signatures). Detection is <sup>37</sup><br>achieved by matching events with these signatures and generating alerts. While signature-based methods have their  $\frac{38}{1000}$   $\frac{38}{1000}$   $\frac{38}{1000}$  $\frac{39}{39}$  limitations, such knowledge could improve the performance of ML-based detection models trained on event data, requiring the ability to extract relevant knowledge and include it in the ML models:

<span id="page-2-4"></span>41 41 Challenge 3. *Extract knowledge (including about threats, malware, and vulnerabilities) and enrich ML-based de-*42 42 *tection models with it.*

<sup>43</sup> In addition to reports, many knowledge bases and formal ontologies can be used to enrich ML models with <sup>43</sup> <sup>44</sup> such knowledge. There are also attempts to extend the coverage domain for such ontologies: one example is the <sup>45</sup> *unified cybersecurity ontology* (UCO) [\[104\]](#page-29-0) and another is the SEPSES knowledge graph [\[57\]](#page-27-6). To represent cyber 46 and  $\frac{1}{46}$  and  $\frac{$ 

<span id="page-2-1"></span><sup>47</sup> 47 <sup>2</sup>Other common reference models are the OODA (Observe-Orient-Decide-Act) loop [\[15\]](#page-26-8) and IACD (Integrated Adaptive Cyber Defense)  $\frac{48}{3}$ framework [\[29\]](#page-26-9).

<span id="page-2-2"></span><sup>&</sup>lt;sup>49</sup><sup>49</sup> <sup>3</sup>There has recently been a vast number of proposals for using *large language models* (LLMs) across MAPE-K. Here, we include what we<sup>49</sup> <sup>50</sup> currently consider the most promising uses of LLMs and refer to [\[14,](#page-26-10) [77\]](#page-28-6) for a more complete discussion.

<span id="page-2-3"></span><sup>&</sup>lt;sup>4</sup>As most events are benign, the base rate fallacy is important in this domain. 51

 1 threat intelligence (CTI), a commonly used schema is *Structured Threat Information eXpression* (STIX) [\[81\]](#page-28-7), with 2 the associated *Threat Actor Context* (TAC) ontology [\[71\]](#page-27-7). A widely used knowledge base for threat actors and 3 attacks is MITRE ATT&CK [\[76\]](#page-28-8). ML, and in particular *natural language processing* (NLP), is being explored for 4 extracting CTI into symbolic forms (e.g. STIX) [\[70\]](#page-27-8) or to map with MITRE ATT&CK [\[64\]](#page-27-9). *Large Language Models* 5 (LLMs) are also explored for this topic [\[46,](#page-27-10) [65\]](#page-27-11), with limitations identified [\[110\]](#page-29-1). However, we are not familiar with 6 approaches to combine and integrate such knowledge with ML models for detection trained on events.

7 7 A different approach to identify malicious behaviour is *cyber threat hunting*. This is a *hypothesis-driven* approach 8 where hypotheses are iteratively formulated (typically using CTI) and validated using event logs, as well as other 9 9 knowledge [\[99\]](#page-28-9). Automating this process is our final challenge for the monitor phase:

<span id="page-3-2"></span>10 10 **Challenge 4.** Automated generation of hypotheses from CTI and validation of hypotheses using observations for  $\frac{1}{11}$  $\frac{12}{2}$   $\frac{12}{2}$  *threat hunting.*

13 13 There are AI-based approaches to facilitate threat hunting [\[79\]](#page-28-10). Most have focused on supporting hypothesis gener-<sup>14</sup> ation by extracting relevant CTI, and using both ML/NLP [\[36\]](#page-26-11) and symbolic AI [\[91\]](#page-28-11). Symbolic AI has been used to 15 15 support validation [\[20\]](#page-26-12).

16 16 *Analyse* The goal of the analysis phase is to understand the nature of the observed alerts, determine possible  $\frac{17}{17}$ business impact and create sufficient situational awareness to support the subsequent pland and execute phases.

19 19 Both malware and benign software continuously evolve. This makes it difficult to separate malicious from benign behaviour [\[33\]](#page-26-7), despite continuous detection engineering efforts improving the capabilities. For example, an update  $_{20}$ to benign software may cause a match with an existing malware signature, and may also show up as an anomaly in  $_{21}$ the network traffic. As a result, most of the alerts are either false or not sufficiently important for further investigation  $\frac{22}{2}$  $_{23}$  [\[17\]](#page-26-6). The analysis phase is, therefore, labour-intensive, where security analysts must plough through and analyse a  $_{23}$ large number of alerts – most of them false – to decide their nature and importance. This could lead to so-called  $_{24}$ <sup>21</sup> alert fatigue among security analysts:

# <span id="page-3-1"></span>26 26 Challenge 5. *The volume of alerts leads to alert flooding and alert fatigue in SOCs.*

 $27$ 28 128 28 Understanding the nature of alerts is important, and studies have shown that a lack of understanding of the  $\frac{28}{28}$ 29 underlying scores, or reasoning, behind the alerts have led to misuse and mistrust of ML systems [\[82\]](#page-28-12). Both studies  $_{30}$  [\[17\]](#page-26-6) and guidance from ENISA [\[33\]](#page-26-7) have highlighted the need for alerts to be reliable, explainable and possible to  $_{30}$ analyse. The use of explainable AI to support this has shown some promise [\[30\]](#page-26-13), and both knowledge graphs [\[17\]](#page-26-6)  $\frac{31}{2}$  $\frac{32}{32}$  and ELWIS have been numbered as promising approaches. and LLMs<sup>[5](#page-3-0)</sup> have been identified as promising approaches.

33 33 An alert is just one observation and needs to be put into a larger context to identify an *incident* and provide nec- $_{34}$  essary *situational awareness* as a result of the analysis [\[34\]](#page-26-14). Such contextualisation includes enriching alerts with  $_{34}$ <sub>35</sub> relevant knowledge from previous incidents, common systems behaviour, infrastructure details, threats, assets, etc.  $_{36}$  The same attack – or the same phase of a larger attack – is likely to trigger many different alerts. Different ML  $_{36}$ techniques, particularly clustering, have been studied to fuse or aggregate related alerts [\[59,](#page-27-12) [105\]](#page-29-2). In addition to  $37$ 38 38 understanding an incident and achieving situational awareness, contextualisation will also help a security analyst  $_{39}$  understand individual alerts. Similar to challenge [3,](#page-2-4) contextualization of alerts will necessarily involve extracting  $_{39}$ 40 symbolic representation from a vast amount of available (and typically unstructured) information. A cyber attack  $\frac{40}{40}$ conducted by an advanced adversary will, in most cases, manifest itself over several phases, creating a need to dis- $_{42}$  cover the relationships (between the alerts) across the different phases of an attack. A common reference model to  $_{42}$ 43 43 relate such phases is the *cyber kill chain*, originally developed by Lockheed Martin and later refined into the *unified* 44 44 *cyber kill chain* [\[89\]](#page-28-13). Other formalisms that enable modelling different phases of attacks include *MITRE Attack* 45 45 *Flow* [\[75\]](#page-28-14) and the *Meta Attack Language* (MAL) [\[52\]](#page-27-13). Different approaches have been studied to relate the different  $_{46}$  phases, including symbolic approaches [\[85\]](#page-28-15), AI planning [\[7,](#page-25-5) [74\]](#page-28-16), knowledge graphs [\[20,](#page-26-12) [60\]](#page-27-14), state machines [\[108\]](#page-29-3),  $_{46}$ clustering [\[44\]](#page-27-15) and statistics [\[46\]](#page-27-10). However, this research topic is considerably less mature compared with ML mod- $_{48}$  els for detection in the monitor phase. We summarise the challenges of combining, understanding and explaining  $_{48}$  $_{49}$  observations in the following challenge:  $_{49}$ 

<span id="page-3-0"></span> $50$ 

<span id="page-4-1"></span>1 1 Challenge 6. *Combine observation with knowledge to analyse, develop and communicate situational awareness.*

 $\frac{2}{3}$  Developing cyber situational awareness requires connecting a plethora of different sources, such as alerts and details <sup>3</sup> Developing eyeer shuunomir uwuress requires connecting a premora so unrerent sources, such as aren'ts and the about infrastructure and threats. There have been proposals to use knowledge graphs to combine these different  $\frac{3}{4}$ sources to support analysis [\[66,](#page-27-0) [100\]](#page-28-0), including explanation [\[17\]](#page-26-6).

 $\frac{5}{2}$  source to support unarysis [co, rooj, mercurity explanation [17].  $\frac{6}{6}$  When an incident is understood and sufficient situational awareness is achieved, a suitable amount of resources have to be allocated to handle the incident. There may be multiple incidents requiring some prioritization between <sup>8</sup> them. This involves understanding the risk and potential impact of the incident, including any mitigating actions that may be taken in subsequent MAPE-K phases:

<span id="page-4-2"></span><sup>10</sup> **Challenge 7.** *Understanding the risk, impact, importance and priority of incidents.*  $10$ 

 $11$  11 <sup>12</sup> *Plan & Execute* The last two phases of MAPE-K, plan and execute, focus on responding to detected incidents.  $_{13}$  This involves finding suitable responses in the plan phase and preparing and executing the response(s) in the execute  $_{13}$ <sub>14</sub> phase. From an AI perspective, research in these phases is not as mature as in the monitor and analyse phases.  $_{15}$  Therefore, we will only focus on the plan phase, which we currently consider to have more interesting AI-related  $_{15}$ 16 16 challenges. To plan a suitable response, two promising AI techniques are *AI planning* (e.g. [\[40\]](#page-26-15)) and *reinforcement*  $_{17}$  *learning* (RL – e.g. [\[50,](#page-27-16) [80\]](#page-28-17)). Each of them has its pros and cons: AI planning requires considerable knowledge  $_{17}$  $_{18}$  and formulation of the underlying environment, whilst reinforcement learning requires a considerable amount of  $_{18}$  $_{19}$  interactions/simulations (often in the millions). In certain cases, a quick response time is necessary, which means  $_{19}$  $_{20}$  this level of interaction would be too time-consuming. When generating response actions, their risk and impact  $_{20}$  $_{21}$  must be taken into account (including the risk and impact of not acting), which is an unsolved problem when using  $_{21}$  $_{22}$  AI. Moreover, when proposing a response action, an AI-generated solution must be able to explain both what the  $_{22}$ 23 23 response action will do and why it is suitable for the given problem:

<span id="page-4-3"></span>24 24 Challenge 8. *Generate and recommend suitable response actions in a timely manner that take into account both* 25 25 *risk and impact and are understandable for a security analyst.* 26  $\sim$  26

27 27 To support such generation, there are several frameworks and formal ontologies that can be used, such as MITRE 28 28 *D3FEND* [\[54\]](#page-27-17), *RE&CT* [\[2\]](#page-25-7) and *CACAO playbooks* [\[72\]](#page-27-18).

29  $\alpha$  11 11  $\pi$   $\alpha$   $\cdots$   $\alpha$   $\cdots$   $\cdots$   $\cdots$   $\cdots$   $\cdots$   $\cdots$   $\cdots$   $\alpha$   $\cdots$   $\cdots$  **Shared knowledge** The 'K' in MAPE-K stands for *knowledge* shared across the phases, and we have, for instance,  $\frac{31}{22}$  knowledge takes different forms and representations (structured and unstructured) and is analysed using different  $\frac{31}{22}$ 32 montengo unos universitas como una representación (su actualmente una universitativa) una islama pode using universitativa techniques (symbolic and sub-symbolic). In addition to consuming knowledge, it is also important to share knowledge edge with key stakeholders, both technical and non-technical [\[32\]](#page-26-16). This may be a report about an incident for internal  $\frac{34}{34}$  $35$  use (e.g. to board members) or sharing threat information with a wider community: seen knowledge about threats and the infrastructure being protected used across different phases. Moreover, this

<span id="page-4-4"></span>36 36 Challenge 9. *Generating suitable incident and CTI reports for the target audience.*

 $37$  37 38 38 To summarise, we have shown the need to learn and reason across MAPE-K and that both symbolic and connec- $_{39}$  tionist AI are being used across the phases. We have identified several challenges, and next, we make the case for  $_{39}$  $A_{40}$  NeSy to address them.

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# <span id="page-4-0"></span>43 43 3. The case for neurosymbolic AI

 45 Kahneman's [\[53\]](#page-27-19) distinction between (fast) instinctive and unconscious '*system 1*' processes from (slow) more 46 reasoned '*system 2*' processes, has often been used to illustrate the NeSy integration of neural networks (system 1) 47 and logical reasoning (system 2). This interdisciplinary approach integrates neural networks adept at learning from 48 vast amounts of unstructured data with symbolic representations of knowledge and logical rules to enhance the 49 interpretability and reasoning capabilities of AI systems. Building on the above analogy, system 1 can, in a SOC, be 50 seen as the ML-based AI used to identify potentially malicious behaviour in the monitor phase. Here, a large amount 51 of noise needs to be filtered out from the large amount of events (thus a need for speed and scalability). System 2

<sup>1</sup> is the reasoning conducted in the analysis phase, which requires deeper insight with the need for scalability less <sup>1</sup> 2 significant. significant.

3 3 This dichotomy of requirements entails that neither end-to-end pure statistical nor pure logical approaches will be <sup>4</sup> sufficient, and a NeSy combination seems ideal. Three commonly used reasons for pursuing NeSy are to design sys-5 5 tems that are *human auditable and augmentable*, can *learn with less* and provide *out-of-distribution generalisation*  $6$  [\[41\]](#page-26-17). We have seen examples of each of these in the challenges described in [§2:](#page-2-0) the use of knowledge to contextu-<sup>7</sup> alise, analyse and explain alerts; generate and explain response actions; learn from (relatively few) incidents; and  $\frac{7}{100}$ <sup>8</sup> handle concept drifts and noise in order to achieve high accuracy of ML models under real-world conditions.

<sup>9</sup> From the challenges in [§2,](#page-2-0) we will here outline a set of NeSy use cases we believe are promising and identify <sup>10</sup> some promising NeSy tools and techniques for each of them. This work is not complete and should be seen as a  $10$ <sup>11</sup> start (see [§5\)](#page-25-0). Moreover, this section is speculative by nature, but we provide some evidence in terms of existing  $11$ <sup>12</sup> work and experiments conducted in [§4.](#page-8-0)  $\frac{1}{3}$  13

<sup>14</sup> *Monitor* The ability to integrate relevant knowledge into ML-based detection models (challenge [3\)](#page-2-4) falls directly <sup>15</sup> under the NeSy paradigm, and could both improve performance under real-world conditions (challenge [1\)](#page-2-5) and help <sup>15</sup> <sup>16</sup> to reduce the number of false alerts (challenge [5\)](#page-3-1): <sup>16</sup>

# <span id="page-5-1"></span>17 17

# 18 18 Use case 1. *Use (symbolic) knowledge of threats and assets to guide or constrain ML-based detection engines.*

19 19  $\frac{20}{20}$  A similar case for such a NeSy use case is made in [\[88\]](#page-28-2). *Logical Neural Networks (LNN)* [\[94\]](#page-28-18) are designed to  $\frac{20}{20}$  $_{21}$  simultaneously provide key properties of both neural nets (learning) and symbolic logic (knowledge and reasoning),  $_{21}$ enabling both logic inference and injecting desired knowledge (e.g. about threats and infrastructure) into the neural  $_{22}$ <sub>23</sub> architecture. In *Logic Tensor Networks (LTN)* [\[12\]](#page-25-1), a membership function for concepts are learned based on both 24 24 labelled examples and abstract (logical) rules. LTN introduces a fully differentiable logical language, called *real*  $logic$ , where elements of first-order logic can be used to encode the necessary knowledge. LTN has been studied to  $25$ 26 detect suspicious behaviour [\[83\]](#page-28-1) and is the topic of one of our experiments in [§4.](#page-8-0)

- 27 In challenge [2,](#page-2-6) we highlighted the need to learn from (relatively small) datasets, which is one of the key features  $27$ 28 of NeSy [41]: 28 of NeSy [\[41\]](#page-26-17):
- 29 29 30 30 Use case 2. *Learn detection models from a limited number of (labelled) incidents*

<sup>31</sup> Additional embedded knowledge in an LNN or LTN may help to reduce training time. *NS-CL* [\[69\]](#page-27-20), which builds<sup>31</sup> <sup>32</sup> models to learn visual perception including semantic interpretation of the images, has shown it can be trained on a<sup>32</sup> <sup>33</sup> fraction of the data required by comparable methods – albeit in a different domain with different data sources. NeSy-<sup>33</sup> based inductive logic programming variants, such as  $\partial ILP$  [\[31\]](#page-26-18), would also be able to learn from small datasets. The <sup>34</sup><br><sup>35</sup> learned logic program will also be inherently explainable (see challenge 6)  $\frac{35}{25}$  learned logic program will also be inherently explainable (see challenge [6\)](#page-4-1).

<sup>36</sup><br>Threat hunting involves generating suitable hypotheses, applying and validating them, then update and iterate  $\frac{37}{2}$   $\frac{37}{2}$  (challenge [4\)](#page-3-2). Work has started investigating LLMs for this challenge [\[87\]](#page-28-19). It has been argued for symbolism in LLMs [\[45\]](#page-27-21), and based on that we define an LLM-based NeSy threat hunting use case:

#### <span id="page-5-2"></span><sup>40</sup> **Use case 3.** *LLM-driven threat hunting using symbolic knowledge and reasoning capabilities.*  $^{40}$  $41$   $41$

42 42 LLMs have been used for hypothesis generation in other domains [\[92\]](#page-28-20), which can be further investigated for threat 43 43 hunting. Hypothesis generation is typically driven by CTI, which can be captured in a knowledge graph. The in-<sup>44</sup> tegration of LLMs and knowledge graphs is an active research field [\[86\]](#page-28-21). In addition, symbolic or computational <sup>45</sup> methods could be used for other steps in the hunting process, including: planning how to answer the hypothesis; <sup>4[6](#page-5-0)</sup> reasoning about available data sources to execute this plan; ensuring correct translation to required query language<sup>6</sup>  $47$  to validate the hypothesis using the observations; and finally, reason about the results from the execution and provide  $47$ <sup>48</sup> input for any refinement of the hypothesis for a new hunting iteration.<sup>48</sup> 49 49

- $50$
- <span id="page-5-0"></span>51 51 <sup>6</sup>Events are stored in a SIEM system, which will have a query language.

1 1 *Analyse* A prominent characteristic of NeSy is its capacity to combine learning and reasoning. Such a combination 2 2 is desirable in a SOC, and our next use case, which cuts across the monitor and analyse phases, addresses several of 3 3 the challenges from [§2:](#page-2-0)

# <span id="page-6-1"></span>4 4 Use case 4. *Incorporate learning of detection models with the ability to reason about their outcomes to understand* 6 6 *and explain their nature and impact.*

<sup>7</sup> In [\[88\]](#page-28-2), the case for such integration of detection and analysis using NeSy is also made. One way to achieve this is <sup>8</sup> to simultaneously train a neural network (for detection) with related symbolic rules that can be used for contextual-9 9 ization, analysis and explanation (challenge [6\)](#page-4-1). Two NeSy techniques that can accomplish this are *Deep Symbolic* 10 10 *Learning (DSL)* [\[26\]](#page-26-19) and *Neuro-Symbolic Inductive Learner (NSIL)* [\[25\]](#page-26-20). *dPASP* [\[39\]](#page-26-21) and *NeurASP* [\[111\]](#page-29-4) are tech-<sup>11</sup> niques based on Answer Set Programming (ASP) [\[16\]](#page-26-22), which seems promising for this use case. *dPASP* is based on <sup>12</sup> furnishing ASP with neural predicates as interface to both deep learning components and probabilistic features in or-<sup>12</sup> <sup>13</sup> der to afford differentiable neurosymbolic reasoning. dPASP is suitable for detecting under incomplete information, <sup>13</sup> <sup>14</sup> abductive reasoning, analysis of competing hypotheses (ACH) [\[47\]](#page-27-22), and what-if reasoning.<sup>[7](#page-6-0)</sup> *NeurASP* improves the <sup>14</sup> <sup>15</sup> results from neural classifiers by applying knowledge-driven symbolic reasoning to them. This is achieved by treat-<sup>16</sup> ing the output from the neural classifier as a probability distribution over the atomic facts, which are then treated in <sup>16</sup> <sup>17</sup> ASP. The ASP rules can also be used to improve the training of the neural networks (use case [1\)](#page-5-1). *DeepProbLog* [\[68\]](#page-27-23) <sup>17</sup> <sup>18</sup> and *DeepStochLog* [\[109\]](#page-29-5) incorporate reasoning, probability and deep learning, by extending probabilistic logic pro-<sup>19</sup> grams with neural predicates created from a neural classifier, and may thus provide the necessary combination of <sup>19</sup> 20 20 learning and reasoning for this use case.

<sup>21</sup> Breaking use case [4](#page-6-1) into smaller sub-cases, the first being extracting symbolic alerts, in order to support alert <sup>21</sup>  $22$  contextualization, analysis and explanation:  $22$ 

<span id="page-6-2"></span>23  $\sim$  23

24 24 Use case 5. *Extracting alerts in a symbolic form.*

<sup>25</sup> In [\[48\]](#page-27-1), symbolic alerts are extracted from a *graph neural network* (GNN) based detection engine. A combination<sup>25</sup> <sup>26</sup> of *GNNExplainer* [\[112\]](#page-29-6) and DL-Learner [\[63\]](#page-27-24) is used to extract the symbolic alerts. The symbolic rules learnt by <sup>27</sup> both DSL and NSIL may also provide such symbolic alert representation, and the use of e.g. ∂*ILP* for detection will <sup>27</sup><br><sup>28</sup> learn symbolic alerts by design *Embed* 2Sym [10] extracts latent concents from a neural <sup>28</sup> learn symbolic alerts by design. *Embed2Sym* [\[10\]](#page-25-2) extracts latent concepts from a neural network architecture, and<sup>28</sup> <sup>29</sup> assigns symbolic meanings to these concepts. These symbolic meanings can then be used to encode symbolic alerts.<sup>29</sup>

<sup>30</sup> A SOC typically receives a large volume of threat intelligence, which is too large to thoroughly analyse manually. <sup>31</sup> Such intelligence is used to contextualise alerts, and it is thus desirable to enrich the SOCs knowledge bases with <sup>31</sup> <sup>32</sup> relevant intelligence reports:  $\sim$  33

<span id="page-6-4"></span>34 34 Use case 6. *Use statistical AI to enrich or extract symbolic knowledge.*

<sup>35</sup> 35 This use case addresses challenge [6.](#page-4-1) In [§2,](#page-2-0) we discussed several approaches to extract knowledge in a suitable <sup>36</sup> symbolic form from reports [\[64,](#page-27-9) [65,](#page-27-11) [70\]](#page-27-8). *STAR* [\[93\]](#page-28-22) is a possible NeSy technique that can be used. It combines  $\frac{37}{27}$   $\frac{1}{27}$   $\frac{1}{27}$  LLMs with ASP, where ASP can be employed to reason over the extracted knowledge, in addition to just extracting  $\frac{38}{38}$ it.

<sup>39</sup><br>This ability to reason is crucial as the intelligence report may be incorrect or superseded for different reasons, <sup>40</sup><br>including underlying (aleatoric) uncertainty, deterioration over time, or from sources one does not fully trust. It may 41 41 also simply not be relevant for our purposes, or more importantly, intelligence reports may conflict with our existing  $\frac{1}{42}$ knowledge or our observations. It would therefore be desirable to quantify and reason about knowledge, including  $\frac{13}{43}$ the level of trust, from both own observations and existing knowledge:

<span id="page-6-3"></span>45 45 Use case 7. *Reason about and quantify knowledge.*

46 46 47 47 This use case is aimed at addressing challenge [7.](#page-4-2) It may play a role in implementing a technique known as *risk-*<sup>48</sup> *based alerting* [\[103\]](#page-28-23), which involves using data analysis to determine the potential severity and impact of alerts and <sup>49</sup> incidents. *Probabilistic attack graphs* [\[43\]](#page-27-25) has been used to add probabilities to CTI. One potential NeSy approach

- $50$
- <span id="page-6-0"></span><sup>7</sup>dPASP can leverage existing LLM-ASP integrations [\[93\]](#page-28-22) to facilitate use case [3.](#page-5-2) 51

 1 for this use case is *Recurrent Reasoning Networks* (RRNs) [\[49\]](#page-27-26). RRNs could be used to train a ML model from ob- 2 servations to reason about our existing knowledge graph, e.g. to quantify or identify inconsistencies. Another NeSy 3 example is *Neural Probabilistic Soft Logic* (NeuPSL) [\[90\]](#page-28-24), where the output from the trained neural networks is in 4 (symbolic) *Probabilistic Soft Logic* (PSL) [\[11\]](#page-25-8), which can be treated by probabilistic graphical models. NeurASP,

5 5 dPASP, DeepProbLog and DeepStochLog may also be applicable here.

6 6 As discussed in [§2,](#page-2-0) a cyber attack conducted by an advanced adversary will consist of multiple phases and the 7 7 ability to relate these phases is essential when developing cyber situational awareness (challenge [6\)](#page-4-1):

#### <span id="page-7-2"></span>8 8  $\frac{1}{9}$  Use case 8. *Relate the different phases of cyber incidents.*

 10 One concrete NeSy use case would be to merge the statistics- and semantics-driven approaches outlined in [\[8\]](#page-25-9). 11 Further, *PyReason* [\[4\]](#page-25-10) enables temporal reasoning over graphical structures, such as knowledge graphs. This can be <sup>12</sup> used to exploit the temporal aspect of relating the different phases. The second experiment in [§4](#page-8-0) addresses this use <sup>12</sup> 13 case by exploring temporal reasoning using a combination of LLMs, temporal logic, ASP and plan recognition. The 14 ontological reasoning supported by RRNs also seems promising for this type of problem.

15 15 *Plan & execute Neurosymbolic reinforcement learning* **(NeuroRL) [\[3\]](#page-25-11) combines the respective advantages of re-**17 motion feature and 11 paramig. Feature can feature with fewer interactions compared with traditional RD by using inherent knowledge, thus making it more applicable than both RL and AI planning when (near) real-time  $\frac{18}{18}$ response is required and a complete model of the environment is infeasible. Moreover, it has the promise of more explainable response actions, whilst a reasoning engine could, in principle, help to take into account both risk and  $\frac{20}{20}$  $\frac{20}{21}$  impact<sup>[8](#page-7-0)</sup>. Thus, this seems like promising approach for challenge [8:](#page-4-3) inforcement learning and AI planning. NeuroRL can learn with fewer interactions compared with traditional RL

22 22 Use case 9. *Generating impact and risk aware explainable response actions in a timely fashion using neurosymbolic* 23 23 *reinforcement learning,*

 $24$   $24$ 25 Neurosymbolic reinforcement learning has been used in offensive cyber security settings for penetration testing<sup>[9](#page-7-1)</sup>  $_{26}$  [\[28\]](#page-26-3). Whilst there are some commonalities with our challenges, defending has their own peculiarities. For example,  $_{26}$  $_{27}$  speed, risk, impact and explainability are more prominent when defending against attacks.

<sup>28</sup> Shared knowledge A widely applied form of symbolic AI in the context of cybersecurity is in semantic ontolo-<sup>29</sup> gies. Ontologies provide a formal and structured way of representing knowledge that both humans and machines<sup>29</sup> 30 can interpret while accounting for interoperability across systems. Built upon symbolic AI principles, ontologies <sup>30</sup> <sup>31</sup> focus on knowledge representation, logic, and reasoning, using well-defined structured models of the world. They <sup>31</sup> <sup>32</sup> define concepts, their composition, and their relationships within a domain, and they provide a clear distinction be-<sup>32</sup> <sup>33</sup> tween the data (and the information itself) and the underlying model that defines how that information is organised, <sup>33</sup> <sup>34</sup> represented, and processed. This paradigm enables model evolution without data disruption, a known limitation of <sup>34</sup> <sup>35</sup> traditional relational models and other data serialization formats that inherently combine representations and data <sup>36</sup> elements. This powerful paradigm allows for a more seamless integration of federated and siloed (in too many cases <sup>36</sup> <sup>37</sup> heterogeneous) data and can provide ensembles of contextual knowledge graphs in support of answering complex<sup>37</sup> <sup>38</sup> questions for decision-making. In addition, ontologies are the backbone of a knowledge base that can guide learning, <sup>39</sup> ensure consistency, facilitate inference, and provide explainability, making neuro-symbolic systems more capable <sup>39</sup> <sup>40</sup> of handling real-world, knowledge-intensive tasks. Our final use case directly addresses challenge [9.](#page-4-4) Cyber threat <sup>40</sup>  $41$  intelligence is commonly shared in both structured and unstructured forms. LLMs are extensively studied for gener- $41$ <sup>42</sup> ating reports and this is also the case for cyber defence [\[77\]](#page-28-6). The generation process is likely to use symbolism (e.g.  $12$ <sup>43</sup> knowledge graphs [\[86\]](#page-28-21)). The reports need to be correct, which is one area symbolic AI can help [\[45\]](#page-27-21). We, therefore,  $43$ <sup>44</sup> rephrase challenge [9](#page-4-4) as a NeSy use case:  $44$ 45 45

46 46 Use case 10. *Generation of incident reports and CTI reports tailored for a given audience and/or formal require-*47 47 *ments, using (symbolic) knowledge and LLMs.*

48 48

<span id="page-7-0"></span><sup>49</sup> <sup>8</sup>We note that there are additional challenges when generating risk and impact-aware responses, such as both deriving the requirements in<sup>49</sup> 50 the first place and representing them in a suitable way. 50

<span id="page-7-1"></span><sup>9</sup>Penetration tests are simulated attacks against the infrastructure and assets being protected, for instance, to identify vulnerabilities. 51

<span id="page-8-0"></span>3 3 To showcase the feasibility of using NeSy for our use cases, we have conducted several experiments addressing 4 different use cases: 4 and  $\frac{4}{3}$  different use cases: 4 and  $\frac{4}{3}$  different use cases:

- $\frac{5}{6}$  In [§4.1](#page-8-1) we address use case [1.](#page-5-1) This is shown by using Logic Tensor Networks (LTN) [\[12\]](#page-25-1) to show how  $\frac{1}{6}$   $\frac{1}{3}$   $\frac{1}{6}$   $\frac{1}{6}$  knowledge in symbolic form can be used to improve an ML-based detection engine as well as improving  $\frac{1}{7}$ explainability.
- 8 8  $\frac{1}{9}$  – In [§4.2](#page-12-0) we address use case [8.](#page-7-2) Here, LLMs and ASP are used to elicit and reason with adversary attack patterns and observed alerts for situational awareness.
- $10$  and  $10$   $\frac{11}{11}$  – In [§4.3](#page-14-0) we address use case [4,](#page-6-1) including elements from the (sub-) use cases [5,](#page-6-2) [7,](#page-6-3) and [8.](#page-7-2) Here, a NeSy solution  $\frac{11}{11}$ 21<br>12 **Exercise of the Emocusym** [10] approach is explored to contextualize areas. That is, we also fish and formalized  $\frac{1}{13}$  domain knowledge to label clusters of embeddings according to what cyber kill chain phase they are likely to based on the Embed2Sym [\[10\]](#page-25-2) approach is explored to contextualize alerts. That is, we use ASP and formalized represent.
- 14 14  $-$  In [§4.4](#page-18-0) we address use case [3.](#page-5-2) Here, we build on [\[19,](#page-26-4) [21\]](#page-26-5) by exploring the integration of LLMs with a symbolic  $\frac{15}{15}$ approach based on knowledge graphs for threat hunting.
- $\frac{16}{17}$  In [§4.5](#page-22-0) we address use case [6](#page-6-4) (with some elements of use case [8\)](#page-7-2). Here, we extend our previous work using  $17$  11 and  $17$  11 and  $17$  12 and  $17$ data-driven enrichment of (symbolic) knowledge [\[101\]](#page-28-4) with experiments using newly released data and explore  $_{18}$ advantages NeSy provides for this challenge.

#### <span id="page-8-1"></span>20  $\sim$  20 21 21 *4.1. LTN for knowledge-aware intrusion detection*



<span id="page-8-3"></span>39 39 Fig. 1. Overview of LTN-based approach

 $_{41}$  An ML-based intrusion detection systems need to learn how to correlate data and their classes<sup>[10](#page-8-2)</sup>, capturing both  $_{41}$  $_{42}$  simple and complex relationships. However, information that is not present or prevalent in the data might not be  $_{42}$ used, even if it is obvious to an analyst. For this reason, we use a Logic Tensor Network (LTN) [\[12\]](#page-25-1) to learn from  $_{43}$ 44 44 data while being guided by expressed knowledge. Most people intuitively know that a vulnerability in Microsoft 45 Word is not a danger for machines without the software installed. Neural networks, on the other hand, need to learn  $45$ <sup>46</sup> this from seeing it repeatedly in the training data. Common sense knowledge like this can easily be expressed as  $47$  logic statements, which are used to help guide the learning of the model. In intrusion detection, analysts often have  $47$ <sup>48</sup> information to help detect that is not expressed explicitly in the logs used by the detection engine. For example,

<span id="page-8-2"></span> $10$ Classes could, for instance, represent malicious or benign data – or specific attack steps or attack techniques. This depends on the type of  $50$ 51 classifier. 51 51 classifier.

49 49

<sup>1</sup> if a piece of software has a known vulnerability, this information might not be represented in the log data. Such 2 2 2 2 2 2 2 additional knowledge can also be encoded into the LTN.

<sup>3</sup> 3 This experiment addresses use case [1](#page-5-1) and is placed in the monitor phase of MAPE-K. Here, the goal is to detect <sup>4</sup> malicious traffic by training LTN-based classifiers to detect two types of malicious traffic: brute force attacks and 5 5 cross-site scripting (XSS) attacks. A *brute force attack* is a trial-and-error approach that, for instance, tries to guess <sup>6</sup> the correct password, while *cross-site scripting (XSS)* attacks essentially inject malicious code into webpages.

<sup>7</sup> This is achieved by training two different LTN-based classifiers: one classifier that separates brute force attacks <sup>7</sup> <sup>8</sup> from benign traffic and one classifier that separates XSS attacks from benign traffic.<sup>[11](#page-9-0)</sup> Both classifiers use aggregated  $8$ <sup>9</sup> traffic in terms of *NetFlow* entries [\[23\]](#page-26-23). A NetFlow entry contains information about traffic between two distinct  $10$  ports on distinct IP addresses for a given protocol within a given timeframe (which may vary). It will typically <sup>11</sup> contain information about the number of packets and amount of data transferred, in addition to a large range of <sup>11</sup> <sup>12</sup> other features. For our experiment, we have used more than 80 different features.

<sup>13</sup> 13 The LTN-based intrusion detector will generate an alert if a NetFlow entry is classified as brute force or XSS. 14 14 This alert will typically be manually analyst by a SOC analyst – or as we will see in other experiments below – 16 16 further enriched by e.g. other NeSy approaches.

An overview of the approach can be seen in [Figure 1.](#page-8-3) As the learning is supervised, the model takes the ground  $\frac{17}{17}$ truth label for each NetFlow entry as input in addition to the NetFlow entries themselves. The main difference from  $_{18}$  $_{19}$  a vanilla neural network is that we encode and provide knowledge that is hard or not possible to learn from the data  $_{20}$  in terms of *real logic* statements [\[96\]](#page-28-25). This could, for instance, be general knowledge, knowledge about the systems  $_{20}$  $_{21}$  being protected or cyber threat intelligence (CTI) about the threat we are trying to detect. The statements are used  $_{21}$  $_{22}$  in the classifier's symbolic part, while the labels and NetFlows are used in its neural part. The model's output is a  $_{22}$  $_{23}$  predicted class for each NetFlow, along with information about whether the classification is in accordance with the  $_{23}$  $_{24}$  provided statements. The LTN provides a classification with improved performance and explainability over a vanilla  $_{24}$ 25 25 neural network.

 26 The experiment consists of two parts: In the first part, a three-layered fully connected neural network is trained 27 and used as a baseline. In the second part, a LTN with the same underlying neural network structure is enriched with 27 28 additional knowledge [\[12\]](#page-25-1). In both cases, 70% of the data is used for training and 30% for testing. The experiment 29 is inspired by [\[83\]](#page-28-1), where LTN is used in a similar fashion to distinguish benign NetFlows from multiple classes 30 of attack NetFlows. Our experiment takes this further by also encoding cyber security knowledge into the LTN and <sup>30</sup> comparing a classifier with and without the knowledge.<sup>[12](#page-9-1)</sup>  $31$ 

<sup>32</sup> We use the CICIDS2017 dataset [\[97\]](#page-28-26) for our experiment. This dataset simulates benign traffic and attacks over <sup>33</sup> five days, varying the attacks performed each day. In our experiment, we use the subset called "Tuesday morning". <sup>33</sup> <sup>34</sup> The labelled flows are categorized into three classes: "Benign", "Web Attack – Brute Force" and "Web Attack <sup>34</sup> <sup>35</sup> - XS". The classes are significantly imbalanced, with 168, 000 flows in the benign class and 2, 159 flows in the <sup>35</sup><br><sup>36</sup> remaining classes. An imbalance between benign traffic and attacks is common in intrusion det <sup>36</sup> remaining classes. An imbalance between benign traffic and attacks is common in intrusion detection. The dataset  $\frac{37}{38}$  is partitioned into a 30/70-split between the training set and the test set. To account for the class imbalance during  $\frac{37}{38}$ <sup>38</sup> training, we undersample the benign class to match the number of samples from the attack classes and the benign 39 39 class. We include all features from the NetFlows into the sample except for the properties *source IP*, *destination IP*, <sup>40</sup> and *source port* as they will cause over-fitting and not generalise well. We one-hot encode the *destination port* with <sup>41</sup> the 22 most common ports being their own feature, while the remaining ports are regarded as "other ports". We also 42 and the contract process of the contract of one hot encode the *protocol* feature. All features are normalized using min-max normalization. Each NetFlow is represented as a vector of length 92. The LTN consists of one predicate for class membership:

#### 45 45  $I(X, Class)$ . 46 47 47  $P(x, class)$ .

<span id="page-9-0"></span><sup>48 &</sup>lt;del>(a) 11</del> 48 (a) 48 (a) 48 (a) 48 (a) 49 (a) <sup>11</sup>We consider training two binary classifiers more realistic than a multi-class approach for this particular problem. However, note that we  $\frac{49}{49}$ also did train a single multi-class network with comparable results.

<span id="page-9-1"></span> $50$  <sup>12</sup>Similar work using LTN for intrusion detection has been in [\[13\]](#page-25-12). Note that this work was published after our initial LTN experiments [\[42\]](#page-26-0),  $50$ 51 which we extend here. 51

 1 This predicate is configured as a fully connected deep neural network with an architecture of 92 input features, two 2 hidden layers of size 256, and an output layer of size one. ELU is used as the activation function of the hidden 3 layers, while sigmoid is used for the output layer [\[24\]](#page-26-24).

 4 Real logic statements are used to shape the training of the neural network. The idea is that such statements should 5 be created by a cyber security analyst and be based upon knowledge about the system, the current threat landscape, 6 and any other relevant information the analyst has. Training consists of updating the neural network *P* to maximize <sup>7</sup> the accumulated truth value of the axioms [\[12\]](#page-25-1). In this experiment, we first define the following axioms:

9 (1) <sup>∀</sup>*<sup>x</sup>* <sup>∈</sup> *<sup>B</sup>* : *<sup>P</sup>*(*x*,Benign) (2) <sup>∀</sup>*<sup>x</sup>* <sup>∈</sup> *BF* : *<sup>P</sup>*(*x*, Brute\_force) (3) <sup>∀</sup>*<sup>x</sup>* <sup>∈</sup> *<sup>X</sup>* : *<sup>P</sup>*(*x*, XSS)

 11 The first three axioms describe how all flows in the training set labeled as a given class (*<sup>B</sup>* : *benign*, *BF* : *brute force*,  $X : xss$ ) should be a member of that class. This encodes the information of the baseline neural net-<br>work with no additional knowledge. We then define the following axioms: 13 work with no additional knowledge. We then define the following axioms:

$$
(4) \quad \forall x \in NWS : \neg (P(x, Bruce\_force) \lor P(x,XSS)) \quad (5) \quad \forall x \in IT : \neg (P(x, Bruce\_force) \lor P(x,XSS)) \tag{15}
$$

<sub>17</sub> The fourth axiom describes how all NetFlows not going to or from a web server *(NWS: Not web server)* cannot be  $_{18}$  a web attack. Both the XSS and Brute force attack in this dataset are for web servers specifically. The information  $_{18}$  $_{19}$  about what is not a web server is knowledge extracted from the topology of the network we are tasked to defend (i.e.  $_{19}$  $_{20}$  the victim of the attack). The fifth axiom defines all traffic between machines in the victim network *(IT: Internal*  $_{20}$  $_{21}$  *traffic*) as not part of an attack. This is because we expect all XXS or brute force attacks to come from outside of the  $_{21}$  $_{22}$  organization's network. The experiments seek to answer to following research question:

 23 *A classifier enriched with knowledge will perform better and provide better insight into what has been* 24 *learnedthan a purely data-driven classifier.*

 $_{26}$  We trained one baseline model and one LTN model for each of the two attack classes. Both the baseline and LTN  $_{26}$  $_{27}$  use same training set and test set, and have the same configuration of the underlying neural network. We trained  $_{27}$  $_{28}$  all models over 80 epochs with a batch size of 250. The results are presented in table [2.](#page-10-0) The results show that both  $_{28}$ solutions have a high recall when it comes to distinguishing benign traffic from attack traffic. Most importantly can we see that the precision of the LTN classifier is more than double the baseline classifier (0.154 vs 0.066 for brute<br>force) (0.104 vs 0.028 for XSS) indicating that adding knowledge can improve classification force) (0.104 vs 0.028 for XSS) indicating that adding knowledge can improve classification.



<span id="page-10-0"></span>37 Fig. 2. Results from LTN Experiment.

 39 Real logic statements in a LTN are an effective way of injecting knowledge into a neural classifier. They can 40 also help in understanding and influencing the model's training and focus. Next we explore different ways the 41 explainability aspects of LTN can be used by a SOC analysts.

 42 During the training of the LTN, the goal is to maximize the aggregated truth of all the provided statements. This 43 is done by deriving the loss of the model from the aggregated truth. Real logic is a fuzzy logic and we would not 44 expect that all statements hold for all cases. After the training is completed, one can analyse how well the rules hold 45 on all the provided training data to provide insights into how the model works. This can also be used as feedback to 46 the analyst to help change or tweak the rules. In figure [3\(](#page-11-0)a), we plot the satisfiability of the five statements on the 47 training set. Here, we can see that, after training, rule four and five are generally satisfied. They are the rules that 48 reduce false positives (false alerts) for the two attack classes. We can also see that the performance for the third rule, 49 which classifies XSS, is significantly lower. This is in accordance with the results in figure [2.](#page-10-0)

 50 When creating real logic statements there is a risk of creating a statement that does not accurately reflect the data. 51 This can be the result of errors made when defining rules, or due to incorrect intuitions. For example, a rule asserting

8 a set of the set of th 10 14 38 1 1 that only mobile phones are targets of attacks, does not accurately capture reality, as computers and other . If a bad 2 2 rule is introduced we would expect the LTN would have a hard time satisfying this rule at the same time as the other 3 3 rules. We can therefore use the low satisfiability of a rule (after training) as an indication that there is a problem <sup>4</sup> with the rule. The fact that the LTN was not able to find a way to make the rule true, is an indication that it does not <sup>5</sup> describe the data correctly. To demonstrate this, we conduct small experiment where we introduce a new rule that is <sup>6</sup> obviously not true stating that all traffic labelled benign should be classified as brute force:

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10  $\mu$  ,  $\mu$  ,  $\tau$  , After training an LTN with this incorrect rule, we can see in figure [3\(](#page-11-0)b) that the satisfiability of the false rule is significantly lower than the other rules.

 $\frac{12}{12}$  In addition to expressing rules, an analyst may be interested in expressing the relative importance of different 13 13 rules. For example, a rule relating to a rare attack with limited consequences may be given a low priority. Conversely, a rule expressing something very prevalent and critical may be prioritised. To reflect this, we add weights to the rules to give a simple way of assigning the importance of a rule compared to the others, where a high weight results in the statement contributing more to the total aggregated truth.

 $_{18}$  To provide additional insights, the analyst can investigate the satisfiability of the different rules for a given Net- $_{19}$  Flow. For the majority of NetFlows, we expect all rules to hold, as this is what the LTN is optimizing for. However,  $_{19}$  $_{20}$  if some rules are not satisfied, we could pass the information on to an analyst to provide additional explanation and  $_{20}$  $_{21}$  context for their analysis.  $_{21}$ 

22  $\sim$  22



<span id="page-11-0"></span>41 41

42 42  $_{43}$  To summarise, this experiment illustrates the potential of using NeSy to embed additional knowledge into ML  $_{43}$  $_{44}$  models. We also see how LTNs can help analysts understand what the model learns and how it predicts. We have  $_{44}$  $_{45}$  showcased that a neural classifier can be improved by adding knowledge in the form of an real value logic. When  $_{45}$  $_{46}$  using the knowledge-enriched LTN, the number of false alerts was reduced without impacting recall. The LTN also  $_{46}$  $_{47}$  provides multiple techniques to improve the model's explainability. By examining the satisfiability of the statements  $_{47}$  $48$  after training, we can gain valuable insight into what the model has learned or what it is not able to learn. With this  $48$ 49 49 information, we can change and improve the defined statements. The satisfiability can also be used to gain insight 50 50 into the model's predictions. This shows promise for using NeSy to enrich ML-based models with (symbolic) 51 knowledge. 51 51 knowledge.

 $2 \times 2$ 

# <span id="page-12-0"></span>1 1 *4.2. LLMs and ASP for situational awareness*

 3 The previous experiment in [§4.1](#page-8-1) provided an example of how alerts can be raised, while we have addressed the 4 need for supporting alert analysis in [§2.](#page-2-0) In this experiment, we demonstrate such analysis by illustrating the use of 5 NeSy to relate different phases of an attack (use case [8\)](#page-7-2). Here, alerts sequenced by time are mapped to adversary 6 attack patterns, gleaned from textual CTI reports into symbolic form using statistical methods (use case [6\)](#page-6-4). The 7 experiment is inspired by existing work such as: neurosymbolic plan recognition [\[6\]](#page-25-13), attack plan recognition [\[7\]](#page-25-5), 8 and the use of LLMs to extract both *linear temporal logic* (LTL) [\[35\]](#page-26-25) and CTI (in the form of MITRE ATT&CK <sup>8</sup> 9 *tactics* or *techniques*) [13](#page-12-1) [\[46,](#page-27-10) [84,](#page-28-27) [113\]](#page-29-7).

10 10 An LLM is first used to elicit formal representations of attack patterns described in CTI reports, affording us 11 11 a rapid way of converting CTI to symbolic knowledge. Here, we use the NL2LTL Python library [\[35\]](#page-26-25) to extract 12 12 representations of attack patterns in LTL*<sup>f</sup>* [\[27\]](#page-26-26), a temporal logic for finite traces. We are using Open AIs GPT-4 13 13 model with few-shot learning. We define a custom pattern template *ExistenceEventuallyOther* to express the LTL 14 property  $\diamond$ *a* ∧ ∘ $\diamond$ *b*. Each prompt parses two lines from the attack description and finds the appropriate ATT&CK 14 <sup>15</sup> technique (from the allowed symbols), and a LTL formula. We combine the formulas from each prompt into one <sup>15</sup> <sup>16</sup> long LTL formula expressing the whole attack pattern. The following is one prompt generated by NL2LTL:

 $17 \qquad \qquad$  17

# 18 18 18 Prompt generated by NL2LTL

19 de jaro - Antonio III e a Santonio de Santonio de Santonio de Santonio de Santonio de Santonio de la 19 20 20 Translate natural language sentences into patterns: 21  $\frac{1}{2}$   $\frac{1}{2}$ 22 **ALLOWED\_SYMBOLS:** T1548 (Abuse Elevation Control Mechanism), T1552 (Unsecured Credentials), 23 23 T1133 (External Remote Service), T1586 (Compromise account) [...] 24 24 ALLOWED\_PATTERNS: ExistenceEventuallyOther

25  $\frac{1}{25}$  25  $\frac{1}{25}$  25 ## Few shot learning example

26 26 NL: The adversary logs into the Kubernetes console.

 $27$  This leads to: The adversary can view plaintext AWS keys in the Kubernetes console.

 $28$  28  $28$ PATTERN: ExistenceEventuallyOther

29 29 SYMBOLS: T1133, T1552

#### 30 30 ## Query

 $\frac{31}{2}$   $\frac{1}{2}$   $\frac{31}{2}$   $\frac{31}{2}$   $\frac{31}{2}$   $\frac{31}{2}$   $\frac{31}{2}$   $\frac{31}{2}$   $\frac{31}{2}$ <sup>32</sup> NL: Attackers leveraged spearphishing emails with malicious links to gain access to the system.

 $33$  This Leads to: Attackers modifies the tty\_tickets line in the sudoers file to gain root access.

35 35  $36$  A conceptual adversary attack pattern, sequencing MITRE ATT&CK techniques is visualized in Figure [4.](#page-12-2)

 $(1550)$   $(1550)$   $(1510)$   $(1050)$   $(1050)$   $(1050)$   $(1050)$  $\{t1556\}$  ...  $\{t1059\}$  ...  $\{t1548\}$  ...  $\{t1059\}$  ...  $\{t1059\}$  ...  $\{t1059\}$  ...  $\longrightarrow \bullet \longrightarrow \dots \longrightarrow \bullet \longrightarrow \dots \longrightarrow \bullet \longrightarrow \dots \longrightarrow \bullet$ 40  $t_i$  . . .  $t_j$  . . .  $t_k$  . . .  $t_l$  40  $t_l$  41  $t_l$  41 41 41  $\text{LTL}_f: \Box(\mathbf{I} \to \circ \Diamond (t1556 \land \circ \Diamond (t1059 \land \circ \Diamond (t1548 \land \circ \Diamond t1059))))$ <sup>41</sup>

<span id="page-12-2"></span>44 44 Fig. 4. Adversary attack pattern

46 46 Each '*txxx*', where *x* is a number, is a unique technique from the ATT&CK framework, I is the initial state, and  $_{47}$   $\Box$ ,  $\circ$  and  $\Diamond$  are the 'always', 'next' and 'eventually' operators in LTL. Next, telingo[\[18\]](#page-26-27), an ASP solver for  $_{47}$ 48 temporal programs, is used to postdict possible attacks. The telingo program encoding the problem is shown 48

49 49

<span id="page-12-1"></span>50 50 <sup>13</sup>A MITRE ATT&CK *tactic* describes why an adversary performs an action, while a MITRE ATT&CK *technique* describes how the action 51 51 is performed [\[76\]](#page-28-8).

1 1 in Figure [6.](#page-13-0) The program details the sequences of observed alerts (lines 5–11), the LTL*<sup>f</sup>* representations of known 2 2 attack patterns (lines 14–21), and the relationships between alerts and ATT&CK techniques (lines 25–28).

<sup>3</sup> 3 3 3 3 The attack patterns in the program are acquired by the elicitation step described above, and the sequences of <sup>3</sup> <sup>4</sup> observed alerts are assumed to come from a SIEM system. That is, alerts produced are in a structured form amenable <sup>5</sup> to be represented as Prolog/ASP terms. We assume that this conversion of alerts to symbolic form (use case [5\)](#page-6-2) exists <sup>6</sup> (see e.g. [\[48\]](#page-27-1)). Furthermore, they are temporally ordered inducing a sequence of alerts (where  $a_x$  is an alert in <sup>7</sup> symbolic form), as shown in Figure [5.](#page-13-1)

<span id="page-13-1"></span>8 a set of the set of th

<span id="page-13-2"></span><span id="page-13-0"></span>



<sup>8</sup> The outcome of the run in this experiment following the program in Figure [6,](#page-13-0) is that there are 2 stable models. <sup>9</sup> This means that it is plausible that the input trace is an instance of the attack plan. Had there been no stable models, <sup>10</sup> the conclusion would have been that this could not have been the case. <sup>10</sup>

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7

# <span id="page-14-0"></span>12 *4.3. Neuro-symbolic alert contextualisation*

<sup>14</sup> Deciding which alerts are important and require attention, and understanding how they belong in the bigger <sup>14</sup> picture, is essential in a SOC. This, however, requires contextualizing alerts with knowledge such as knowledge  $15$ <sup>16</sup> about the systems and networks in which the alerts were raised, cyber threat intelligence, and background knowledge <sup>17</sup> accumulated by analysts over time. This is illustrated in Figure [7,](#page-14-1) where the context allows an analyst to follow a <sup>18</sup> continuous path through alerts and log events.  $\frac{19}{19}$  19



<span id="page-14-1"></span> 32 Fig. 7. Illustration of how context contributes to create a continuous path through logs and alerts. 33

 34 In this experiment, we assume both rule-based and anomaly-based alerts, which differ widely in contextual rich- 35 ness, and we aim to classify these alerts by the cyber kill chain step to which they are likely to belong. The experi-36 ment mainly addresses use case [4,](#page-6-1) but also includes aspects of use cases [5,](#page-6-2) [7](#page-6-3) and [8.](#page-7-2)

<sup>37</sup> Rule-based alerts are generally contextually richer than anomaly-based alerts; the former are mostly hand-crafted <sup>37</sup> <sup>38</sup> and contextualized with descriptive knowledge as to what type of suspicious behaviour it detects (e.g. which MITRE <sup>39</sup> ATT&CK technique the alert indicates), while the latter are generally more primitive alerts that flag any abnormal <sup>39</sup> <sup>40</sup> attribute values (that deviate from normally seen values during training). These are thus less descriptive with regards <sup>40</sup> <sup>41</sup> to what behaviour is detected. Hence, it is for example easier to associate cyber kill chain phases with rule-based<sup>41</sup> alerts than with anomaly-based alerts. <sup>[15](#page-14-2)</sup> On the downside, contrary to anomaly-based alerting, rule-based alerting  $42$ <sup>43</sup> is not able to detect novel and previously unseen suspicious behaviour. Both types of alerts are thus useful when <sup>43</sup> detecting cyber attacks.

#### <sup>45</sup> For this experiment 46

 47 *we wish to classify alerts according to cyber kill chain steps, yet we have alerts with a highly varying degree of* 48 *contextual richness on which to do so.*

<span id="page-14-2"></span> <sup>15</sup>We note, however, that a detection rule can be (and often is) an indicator of more than one TTP/cyber kill-chain phase and therefore  $50$ 51 non-trivial to uniquely identify it.

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<span id="page-15-0"></span> $\frac{34}{2}$  34  $\frac{34}{2}$  34  $\frac{34}{2}$  34  $\frac{34}{2}$  34  $\frac{34}{2}$  35  $\frac{34}{2}$  35  $\frac{34}{2}$  35  $\frac{34}{2}$  36  $\frac{34}{2}$ Exemplifying (a), the cluster that contains an alert generated by a rule that detects MITRE ATT&CK technique T1548 should ideally be labelled *Lateral Movement*. Exemplifying (b), if *alert*<sub>1</sub> ∈ *cluster*<sub>1</sub> and *alert*<sub>2</sub> ∈ *cluster*<sub>2</sub>,  $\frac{36}{36}$ they both involve username *user*, and *alert*<sub>1</sub> happens before *alert*<sub>2</sub>, then *cluster*<sub>1</sub> should ideally be labelled with  $\frac{37}{27}$ 38 38 a cyber kill chain stage that occurs before the label assigned to *cluster*2, e.g. *Lateral Movement* before *Privilege*  $\frac{23}{39}$  Escuador.  $\frac{3}{39}$ *Escalation*.

Turning to the technical details, we follow the approach presented in [\[10\]](#page-25-2), referred to as  $Embed2Sym$ , where a  $_{41}$  neural perception and reasoning component is combined with a symbolic optimization component for extracting  $_{41}$  $_{42}$  learned latent concepts. For the neural component, perception and reasoning is conducted in two separate stages. <sup>43</sup> The latter stage (reasoning) is designed to solve a downstream task, whereas the perception stage creates vector <sup>44</sup> embeddings of the input data. By solving the downstream task, the reasoning stage discovers structure in the data <sub>45</sub> relevant to the domain. This is fed back to the perception stage, influencing the vector embeddings. Finally, the <sub>45</sub>  $_{46}$  embeddings are clustered, and symbolic optimization using ASP is used to label the clusters according to the latent  $_{46}$  $\alpha$ 47 **Concepts.**  $\alpha$ 48 This experiment is built upon logs and alerts from the dataset described in [\[61\]](#page-27-27) and [\[62\]](#page-27-28). The logs and alerts are 48 concepts.

49 49 collected from a testbed emulating a small enterprise where a multi-step attack is being performed. The data also 50 50 includes ground truth, making it possible to see exactly where in the logs and alerts the attack is captured and also 51 51 what hostile activity gave rise to each of these log lines and alerts.

1 1 We transform this data into graph form, and we will henceforth refer to the graph representation of each log line 2 2 as one *log graph* and the graph representation of each alert will be considered as one *alert graph*. The whole dataset, 3 3 then, is represented as a union of the log and alert graphs. The latent concepts of interest are cyber kill chain stages, 4 4 and the cyber kill chain stages in the experiment is based upon the stages used in the attack described in [\[61\]](#page-27-27):  $\frac{5}{10}$   $\frac{1}{10}$   $\frac{1}{10}$  6 6  $\frac{7}{2}$  2. Obtained at 1. 8 8 9  $\sigma$  1. 10 10 11 11 Our instantiation of Embed2Sym is shown in Figure [8.](#page-15-0) The neural processing is conducted in two stages: 1. Reconnaissance 2. Initial intrusion 3. Obtain credentials 4. Privilege escalation 5. Lateral movement

- <sup>12</sup> 1. First, training an embedding function (which would be the perception stage in Embed2Sym) and a classifier <sup>12</sup> 13 (reasoning stage in Embed2Sym).
- <sup>14</sup> 2. Then, in the downstream task for the classifier, classify the alert log graphs according to hostile activity, <sup>15</sup> utilizing the ground truth labelling in the data. Notice here that as each alert is related log lines, each alert 16 16 graph also includes a log graph.  $\frac{17}{17}$  17

 $_{18}$  In the training of the neural processing these two stages interact, meaning that the trained embedding function is  $_{18}$ 19 19 influenced by the classification stage.

 $_{20}$  For the next step in the process, we consider the set of alert graphs that we wish to analyse. Using the embedding  $_{20}$  $_{21}$  function, these alert graphs are transferred into the embedding space, where they are clustered. The intuition behind  $_{21}$  $_{22}$  this step is that the downstream task of classifying the alert graphs according to the actual hostile activity should  $_{22}$  $_{23}$  force the embeddings of alert graphs from the same stages of the attack closer together in the vector space.

 $_{24}$  The final step is to apply symbolic reasoning, utilizing formalized domain knowledge, to label the clusters ac- $_{25}$  cordingly. The task is encoded as an ASP program, shown in Figure [10,](#page-17-0) and the clustered (alerted) logs as ASP facts  $_{25}$ 26 as shown in Figure [9.](#page-16-0)

28 28 29 2 | happensAt (  $log 1$ , 100000).<br>29  $3$  | dst\_host ( $log 1$ , "10.0.0.1"). 30 30  $31 \quad 5 \quad \text{detected (log1, "T1000").}$   $31$ 32 7 dst\_user(log1, "Jack").<br>8 src\_host(log1, "192.168.0.10").  $log_i$  in  $_{\text{cluster}}$  ( $log1$ , cluster 1).<br>hannens At ( $log1$ , 100000). 4  $\begin{bmatrix} 5 \\ 6 \end{bmatrix}$  s r c \_ u s e r ( log1 , "John" ) .  $dst_use$  ( $log1$ ,

# <span id="page-16-0"></span>35 35 Fig. 9. ASP instance encoding

 37 Starting with the encoding of the instance data, lines 1-3 in Figure [9](#page-16-0) encode that a log belongs to a cluster, that 38 it happened at a certain unix epoch time, and was logged on a specific host, respectively. Line 5 encodes that the 39 alerted log was generated by a rule that detects instances of MITRE ATT&CK tactic T1000, while lines 6-8 encode 40 the ip-address that initiated the process that was logged, the username was associated with the logged event, and 41 the username that originally initiated the logged event (e.g. a *su* operation), respectively. Lines 1-3 encode facts that 42 all logs will contain, while lines 5-8 depend on the underlying log event type (e.g. network traffic log or process 43 execution log).

44 44 Proceeding to the encoding of the task itself, shown in Figure [10,](#page-17-0) the first part establishes some basic cyber kill 45 45 chain and TTP domain knowledge. That is, lines 2-4 define cyber kill chain phases, and their relative ordering in the 46 46 chain, while lines 6-10 map MITRE ATT&CK techniques to the cyber kill chain phases used in our experiment.

47 47 The next part introduces rules pertaining to the order and shared features of log events. The rule in line 13 48 48 captures the temporal order of log events, while lines 13-28 capture shared features between logs, such as sharing 49 49 users, source and destination addresses etc.

50 50 The following part, lines 31-34 deals with defining what constitutes labels and clusters, while lines 37-38 are 51 51 responsible for allocating labels. That is, the choice rule in line 37 ensures that each cluster is assigned a label,

<span id="page-17-1"></span><span id="page-17-0"></span>

<sup>1</sup> and line 38 ensures that each cluster is only assigned a single label. Line 39 is a convenience rule that in practice <sup>1</sup> 2 2 classifies a log based on the assigned label of the cluster it belongs to. Finally, lines 43-50 capture the two weak 3 3 constraints that encode the optimization tasks that is described in the beginning of this section.

 4 For the experimental run itself, we clustered 1900 alerts from the dataset into 6 clusters (number of cyber kill chain 5 steps plus one 'benign'). Of these 1900 alerts, 290 had information that associated them with MITRE ATT&CK 6 tactics. For convenience, we identified the clusters with meaningful names in order to make validation easier (e.g. 7 cluster2 was named "webshell" ). We then ran the ASP encoding of the task and instance data through the Clingo 8 8 ASP grounder and solver [\[38\]](#page-26-28), which was able to classify the labels correctly, as shown in Figure [11.](#page-17-1)

9 9 Although this experiment was limited to detecting one specific instantiation of a cyber kill chain within a gen-<sup>10</sup> erated but realistic dataset, we believe that the results indicate that the approach is feasible for classifying alerts <sup>10</sup> <sup>11</sup> according to cyber kill chain steps even when contextual information regarding the alerts varies widely.

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# <span id="page-18-0"></span>13 13 *4.4. NeSy-driven threat hunting*

15 15 The previous experiments have focused on intrusion detection and subsequent analysis of the raised alerts. This <sup>16</sup> experiment focuses on a different approach to discovering malicious behaviour called threat hunting (see challenge <sup>16</sup> <sup>17</sup> [4\)](#page-3-2). The experiment addresses use case [3](#page-5-2) and explores the efficacy of leveraging LLMs to develop a taxonomy of <sup>17</sup> <sup>18</sup> behavioural indicators for the (symbolic) *indicators of behavior* (IOB) approach to threat hunting [\[19,](#page-26-4) [21\]](#page-26-5). This sym-<sup>18</sup> <sup>19</sup> bolic threat hunting approach utilises an ontology and semantic reasoning to infer a set of contextualised adversarial <sup>19</sup>  $20^{\circ}$  behaviors across a series of logged security event data. Whilst this IOB-concept has previously been demonstrated  $20$ 21 21 [\[19,](#page-26-4) [21\]](#page-26-5), it lacks a taxonomy of behaviours and reusable IOB identifiers.

<sup>22</sup> Natural language processing techniques have been utilised for extracting Indicators of Compromise (IOCs) from <sup>22</sup> <sup>23</sup> CTI Reports [\[67\]](#page-27-29) and, more recently, extended to the utilisation of LLMs for extracting IOCs from CTI reports<sup>23</sup> <sup>24</sup> [\[106\]](#page-29-8). Here, we explore the implementation of LLMs for developing an IOB taxonomy. The utilisation of LLMs for <sup>24</sup>  $25$  generating detection logic from a conceptualised task has been demonstrated in industry [\[98\]](#page-28-28). Motivated by this, in  $25$ <sup>26</sup> this experiment we explore the automated development of rule-based reasoning into our taxonomy.

<sup>27</sup> Threat hunting involves the generation of suitable hypotheses, followed by applying and then validating the <sup>27</sup> <sup>28</sup> hypotheses (see challenge [4\)](#page-3-2). This experiment uses a scenario-driven approach to IOB development, where the <sup>28</sup> <sup>29</sup> scenario is a hypothesis of describing what an adversary, tool or general user is trying to achieve. For a given <sup>29</sup> 30 scenario, the LLM is tasked with generating a set of low-level behavioural indicators that analyse syntax, commands <sup>30</sup> <sup>31</sup> and other properties at a low-level of details and reason over these indicators to infer a higher level of abstraction.<sup>31</sup>

<sup>32</sup> A simple example of such a scenario is notepad.exe being launched by the Windows built in *system user*<sup>[16](#page-18-1)</sup><sup>32</sup> <sup>33</sup> and then establishing a network connection. This example is a set of low-level behaviours. By combining these <sup>33</sup> <sup>34</sup> individual behaviours, a higher level of abstraction can be inferred as an interactive tool being launched by the <sup>34</sup> <sup>35</sup> system user for the purpose of networking. We can chain this behaviour together with other inferred behaviours to <sup>35</sup> <sup>36</sup> 36 get an even higher level of abstraction.

<sup>37</sup> 37 37 To semi-automate this scenario-driven approach to developing an IOB taxonomy, we require an LLM that can:

- 38 38  $39 \rightarrow$  Contextualise elements of the cybersecurity domain.
- $_{40}$  Contextualise how adversaries behave.
- $_{41}$  Generate behavioural scenarios and transform these scenarios into a chain of events.
- $_{42}$  Contextualise how tools, systems or programs operate in a given scenario.
- $_{43}$  Generate a set of reusable IOB identifiers.
- <sup>44</sup> Relate low-level security events together to form a higher level of abstraction and context.
- 45 45 Transform an IOB scenario into a symbolic representation.
- $_{46}$  Create the detection logic for low-level events as SWRL<sup>[17](#page-18-2)</sup> rules.
- $_{47}$  Be both granular and descriptive to provide context commonly missing from MITRE ATT&CK technique  $_{47}$  $_{48}$  procedures [\[21\]](#page-26-5).  $_{48}$
- 49 49

<span id="page-18-1"></span>50 50 <sup>16</sup><https://learn.microsoft.com/en-us/windows/security/identity-protection/access-control/local-accounts>

<span id="page-18-2"></span>51 51 <sup>17</sup>https://www.w3.org/submissions/SWRL/

 1 These requirements are a mix of concepts and subject areas, where tailored LLMs may struggle to fulfill some 2 requirements and excel in others. As a results of this, we primarily focus on general-purpose LLMs rather than 3 purpose-built LLMs. We compare the following models for their ability to semi-automate the development of an 4 IOB taxonomy:

- $\frac{5}{2}$   $\frac{5}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{5}{2}$   $\frac{5}{2}$   $\frac{5}{2}$   $\frac{1}{2}$   $\frac{1}{2}$  – GPT4-Omni
- $\frac{6}{6}$   $\frac{1}{6}$   $\frac{1}{6}$  – GPT3.5-Turbo
- 7  $-$  Llama 3.2-3b<sup>[18](#page-19-0)</sup>
- $8 \times 10^{10}$  8  $\frac{9}{9}$   $\frac{222222}{9}$   $\frac{9}{9}$  $-$  SecurityLLM<sup>[19](#page-19-1)</sup>

 10 The first three are general purpose, while the last model is purpose-built for cyber security. Various GPT-models 11 have been used in the cyber security domain for a variety of purposes[\[78\]](#page-28-29), including payload generation for offensive 12 security tasks, leveraging knowledge from the MITRE ATT&CK framework and detection engineering. Llama 12 13 has been available for research use [\[73\]](#page-27-30), and SecurityLLM is based on Llama with the intent to provide cyber 14 security guidance [\[115\]](#page-29-9), including threat hunting, cyber kill chains and MITRE ATT&CK. Both Llama 3.2-3b and 15 SecurityLLM were run offline for this experiment.

 16 The scale of symbolic security event data makes it inefficient to process line-by-line via an LLM, due to context <sup>17</sup> size and memory limits. To illustrate, the symbolic event data file generated from a single node in an emulated attack <sup>17</sup> scenario used for our experiment contains 490, 248 lines, and 24, 161, 441 characters. Instead, we leverage the LLM 18<br>to generate JOB scenarios with relevant rule based detection logic, which utilise a reasoning engine fo 19 to generate IOB scenarios with relevant rule based detection logic, which utilise a reasoning engine for decision 20 making. We define a set of constraints through prompt instruction and by embedding tasks within the message to 21 the model to generate these scenarios. 22

- 22 LLMs perform more accurately when prompts utilise chain-of-thought prompting [\[107\]](#page-29-10) and least-to-most prompt- 23 ing [\[114\]](#page-29-11), which we combine in a hybrid approach. Chain-of-thought prompting is used to create a set of behaviors, 24 an abstract definition, a summary, detection logic and the semantics are different concepts. Least-to-most prompt- 25 ing is used to create sub-tasks for the model to maintain accuracy and reduce the risk of LLM hallucination. Each 26 sub-task has an updated prompt instruction set. Each model is tested without a system prompt. The GPT-models 27 are non-configurable, hosted by the OpenAI, and operated in the web browser. Therefore, no configurations are 28 available to share. Llama and SecurityLLM are open and their configurations are included during assessment. 29 Each model has two tasks:
- 30 1. Create the IOB scenario.
- $\frac{31}{22}$  2. Create the symbolic representation.  $\frac{22}{32}$   $\frac{22}{32}$   $\frac{32}{32}$

 33 The prompt hand task specification is developed based on the requirements for symbolic threat hunting as elucidated 34 above, and shown in figure [13.](#page-21-0) Here, prompt instructions (A) and (B) are used for generating IOB scenarios and 35 sub-tasks, while (C) and (D) are used for the generation of symbolic representation.

<sup>36</sup> *GPT4-Omni* was the best-performing model. Without a system prompt, it produced various IOB scenarios and <sup>36</sup> <sup>37</sup> transformed these into a taxonomy. Like most of the models, it arbitrarily chose an IOB ID rather than generating the 38 same each time when a system prompt was not provided. The model worked best with a system prompt, producing 38 39 consistent IOB scenarios that can be concatenated into a behavioural taxonomy. An example scenario output by 40 GPT4-Omni can be seen in figure [13.](#page-21-0)

 41 The scenario in figure [13](#page-21-0) creates the top-level behaviour *H01 ("Data Exfiltration via Command Prompt")* and 42 generates a set of associated behaviours for this scenario. This is the optimal output expected from the LLM. Unlike 43 Llama, this model was capable of producing an SWRL rule-set based on the possible command examples present in <sup>44</sup> the IOB scenario. However, without the contextualised prompt instructions, it would create its own taxonomy. In-<sup>45</sup> stead of using SWRLs built-in regular expressions<sup>[20](#page-19-2)</sup> to trigger within the commandLine data property, it preferred <sup>45</sup> 46 to create a commandLine class and reason over a hasCommand relationship. After defining the scope in the <sup>47</sup> prompt instruction and stating the task, it was capable of correctly generating the SWRL relationships. An example 48

- <span id="page-19-0"></span>49 <sup>18</sup><https://huggingface.co/meta-llama/Llama-3.2-3B>
- <span id="page-19-1"></span>50 <sup>19</sup><https://huggingface.co/ZySec-AI/SecurityLLM>
- <span id="page-19-2"></span>51 <sup>20</sup>https://www.w3.org/submissions/SWRL/#8

#### 2 and  $\frac{1}{2}$  and  $\frac{1$  $\frac{1}{3}$  (A) Prompt Instruction for creating an IOB scenario

- <sup>4</sup> I want you to use a scenario-based threat hunting method for high-level abstractions.
- <sup>5</sup> All scenarios are post-compromise scenarios. The threat actor has access to the network. <sup>6</sup> Atomic level / Low level behaviors require a detection analytic.
- $7\,$  A detection analytic analyses the data logged by Sysmon in the Sysmon schema.
- <sup>8</sup> Bocus on the context that commands, parameters and syntax are trying to achieve.
- <sup>9</sup> Pocus on the context of these commands, parameters and syntax as a chain of events.
- <sup>10</sup> **Focus on Windows enterprise environments.**<sup>10</sup>
- <sup>11</sup> Provide an extensive taxonomy rather than a few examples. The same of the
- <sup>12</sup> **12 Behaviors should focus on common behaviors associated with adversaries.**
- <sup>13</sup> **Summarise with a table at the end.** <sup>13</sup>

#### 15 15 16 16 (B) Tasks Instruction for creating an IOB scenario

<sup>17</sup> I want to create a taxonomy of adversarial behavioral indicators. Do not repeat the MITRE ATT&CK frame-<sup>18</sup> work, I want to compliment it with more detailed levels of abstraction. This is a more detailed level of ab-<sup>19</sup> 19 straction of what an adversary is trying to achieve over a chain of events.

- <sup>20</sup> Por this task focus on behaviours related to command prompt and how and adversary can leverage com-<sup>21</sup> mand prompt for its goals. Focus on the relation command prompt has with other aspects of adversarial <sup>21</sup> 22 behaviours 22 behaviours.
- <sup>23</sup> 23 This taxonomy and the behaviors is a tiered approach where very low level atomic behaviors are sub behav-<sup>24</sup> iors of more abstract concepts. Several medium level behaviors may form a higher level abstraction which <sup>24</sup>  $25$  is the adversaries main goal.  $25$
- <sup>26</sup> Be detailed with the high level abstraction, model it as a scenario and how an adversary may achieve it <sup>27</sup> through its sub behaviours. The high level abstraction should be a reasoned chain of sub behaviors.
- <sup>28</sup> 28 **28 Each behavior has a behavior ID value assigned to it. Prefix with a behavior category and suffix with a <sup>28</sup>** <sup>29</sup> 129 number value. Provide detection analytics for the low level behaviors where possible.<sup>29</sup>
- <sup>30</sup> Summarise at the end with a table with the following: Behavior ID, Description, Commands where relevant <sup>31</sup> and Detection Analytics **31** 32 and the state of the state of

#### $\overline{\phantom{a}}$  33  $\overline{\phantom{a}}$  33  $34$  (C) Prompt Instruction for transforming an IOB detections into SWRL syntax

35 and the contract of the con  $\frac{36}{36}$   $\frac{36}{36}$   $\frac{36}{36}$ Use the SWRL syntax for reasoning rules.

- <sup>37</sup> <sup>2</sup> Command Line is a dataproperty named "commandLine" in the ontology.
- $38$  A process is a member of the "Image" class.
- <sup>39</sup> <sup>A</sup> process individual will have the data property "commandLine" and contain some string to check.
- 40 **The ontology prefix is "threat".** And the ontology prefix is "threat".
- $\frac{41}{41}$  Latin Denavior ID is a crass. Each Behavior ID is a class.

# 43 43 (D) Task Instruction for transforming an IOB detections into SWRL syntax

44 and the contract of the con  $\frac{1}{45}$  I will represent an example SWRL rule. Can you transform the example into an SWRL rule for each indi- $\frac{46}{46}$  vidual command where following vidual command where relevant.

47 47 *Image*(?*e*) <sup>∧</sup> *commandLine*(?*e*, ?*c*) <sup>∧</sup> *swrlb* : *contains*(?*c*, "*nc* <sup>−</sup> *<sup>u</sup>*/*server*/*share*") <sup>→</sup> *LM* <sup>−</sup> <sup>1</sup>*A*(?*e*)

49 49 Fig. 12. Prompts used for NeSy-driven threat hunting. $\sim$  50  $\sim$   $51$  51



<span id="page-21-0"></span> $_{22}$  Fig. 13. An example scenario generated by GPT-4 Omni for generating an IOB taxonomy. This scenario is transformed into an OWL ontology  $_{22}$ 23 and processed by a reasoning engine. SWRL reasoning logic is generated from the list of commands.



<span id="page-21-3"></span><span id="page-21-2"></span><span id="page-21-1"></span>

<sup>50</sup> <sup>22</sup>The following notable settings were used: 28 discrete model layers, three CPU threads, the temperature was 0.5 and the context length was <sup>50</sup> 51 8, 192. , <sup>192</sup>.

<span id="page-22-3"></span><span id="page-22-2"></span><span id="page-22-1"></span><span id="page-22-0"></span>



<span id="page-23-2"></span>48 48

<sup>49 &</sup>lt;sup>25</sup> 25 *Althour United States for the channel* defense to be included information that the indicated continued detect full for more included to the states of the  $^{49}$   $^{25}$ [https://github.com/center-for-threat-informed-defense/technique-inference-engine/blob/main/data/combined\\_dataset\\_full\\_frequency.json](https://github.com/center-for-threat-informed-defense/technique-inference-engine/blob/main/data/combined_dataset_full_frequency.json )  $^{26}$ <br>50  $^{26}$ https://github.com/mnemonic-no/provreq 51 51 <sup>27</sup>[https://github.com/mnemonic-no/provreq-mcmc](https://github.com/mnemonic-no/provreq-mcmc )<sup>26</sup>[https://github.com/mnemonic-no/provreq](https://github.com/mnemonic-no/provreq )

<span id="page-23-3"></span><span id="page-23-1"></span><span id="page-23-0"></span>

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<span id="page-24-0"></span><sup>17</sup> Fig. 17. Box plot with interquartile range 1.5, showing the original data set to the left and the TIE data set to the right. The data used to <sup>17</sup> create the box plot is the highest Markov chain transition probability for each ability. The outliers close to 1.00 are abilities where either a 18<br>cincle technique was observed or where a single technique had an overwhelm  $_{19}$  single technique was observed or where a single technique had an overwhelming number of observation compared to the other techniques. The  $_{19}$ outlier techniques for the original data set were Process Discovery (T1057), Container and Resource Disvocery (T1613), and Gather Victim Org 20  $^{21}$  Share Discovery (T1135), Modify Authentication Process: Network Device Authentication (T1556.004), and Gather Victim Org Information:  $^{21}$ 22 22 Business Relationships (T1591.002). Information: Business Relationships (T1591.002), while the outlier techniques for the TIE data set were Process Discovery (T1057), Network

 $23$ 24 24

 $^{25}$  determine the most likely technique prior to the observed technique. Our conclusions in [\[101\]](#page-28-4) were that this ap- $\frac{26}{25}$  proach is able to determine the prior technique with high probability, but if we try to determine a long attack chain,  $27$   $27$ e.g. from observed exfiltration all the way back to initial access, then the most likely attack chain still has a very  $\frac{28}{28}$ low probability. The example given for *Exfiltration over C2 Channel* (T1041) had a probability  $p = 0.0202$ , which  $30<sub>30</sub>$  is too low to be useful to an incident responder. In [\[101\]](#page-28-4), we speculated that a larger dataset might improve the  $30<sub>30</sub>$ 31 31 performance for long attack chains.

32 32 After running the same experiments on the TIE dataset, our results are similar. In one of the examples from [\[101\]](#page-28-4), <sup>33</sup> we see a clear improvement in the probability when we try to predict the prior technique: the most probable attack<sup>33</sup> chain for the technique *User Execution* (T1204) had the probability  $p = 0.6977$  in [\[101\]](#page-28-4), while with the TIE data <sup>34</sup><br><sup>35</sup> <sup>35</sup> set this increased to  $p = 0.8086$ . In general, however, we see lower probabilities with the TIE dataset compared <sup>35</sup> <sup>36</sup> with the dataset in [\[101\]](#page-28-4), e.g. with the *Exfiltration over C2 Channel* (T1041) example above. On closer examination, 37 37 the reason for this result is that the TIE dataset is more varied than our original data set as it covers a much larger  $_{38}$ <sup>39</sup> 39 11 number of techniques, and the technique observations are more evenly distributed.

<sup>40</sup> <sup>40</sup> To illustrate the difference between the datasets, we extracted the maximum Markov chain transition probability 41 41 for each of the abilities in the transformed dataset and created a box plot, shown in Figure [17.](#page-24-0) The plot shows that the <sup>42</sup> TIE dataset has a lower median than the original data set, which means that in general a long attack chain generated <sup>42</sup> <sup>43</sup> from the TIE dataset will have a lower probability than one created from the original data set (used in [\[101\]](#page-28-4)).

<sup>44</sup> Our conclusions from [\[101\]](#page-28-4) are still valid after testing our tools on the TIE dataset: we are able to answer the  $\frac{45}{10}$  questions in the introduction. However, our remarks that the low probability of long attack chains due to a lack 46  $\frac{1}{2}$  1.  $\frac{1}{2}$  of training data are not valid. Attackers are different, and they use a varied set of techniques. Furthermore, new  $\frac{47}{47}$ techniques are added to ATT&CK with each new revision. This leads us to conclude that our approach is unlikely <sup>49</sup> to give useful results for very long attack chains, and that our tools should rather be used iteratively during incident 50 50 response: predict the most likely prior step, investigate, and then repeat the process once the prior attack step is 51 confirmed. 51 51 confirmed.

 $2 \times 2$ 

# $1 \quad 5.$  Conclusion  $1$

 3 Our main goal with this paper has been to showcase and demonstrate through experiments the possibilities for 4 NeSy in cyber security, focusing on problems within SOCs. We hope this will help stimulate a concerted effort in 5 studying NeSy in this domain. The use of NeSy in cyber security is in its infancy, with some work having appeared 6 over the last few years, including using NeSy for detection [\[83](#page-28-1)? ], generating symbolic alerts [\[48\]](#page-27-1) and extracting 7 semantic knowledge from reports [\[70\]](#page-27-8).

8 We have demonstrated that a considerable amount of symbolic and statistics-based AI is studied in SOC settings, 9 and using it in real-world settings presents several challenges. We believe NeSy can address many of these chal- 10 lenges. Others have made some of the same points [\[51,](#page-27-2) [88\]](#page-28-2), but not to the extent as we do here. We have contributed 11 by defining a set of NeSy use cases and identifying promising NeSy approaches that serve as a starting point –several 12 of them have been demonstrated in our experiments, which are the main new contributions of this paper compared 13 with [\[42\]](#page-26-0). This work is just a start, and we both hope and expect that many new use cases and promising NeSy 14 approaches that we have not covered here will appear in the not-too-distant future. The use cases and experiments 15 provide a starting point for such future work. A challenge with AI in the cyber security domain is available datasets. 16 Due to issues such as privacy, confidentiality and lack of ground truth, researchers tend to use synthetic data, which 17 has their limitations [\[9,](#page-25-4) [55\]](#page-27-5). Furthermore, such datasets tend to focus only on detection (monitor phase), containing 18 only events, and lack the additional (symbolic) knowledge which is important in SOCs and for our use cases. An 19 important first step will be to develop synthetic datasets containing both events for detection and necessary knowl- 20 edge in order to address the use cases. This can either be achieved by extending existing "detection datasets" [\[58\]](#page-27-4) 21 with the necessary knowledge or by developing new "NeSy datasets" from scratch.

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